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## Conoscopic image of a biaxial nematic phase in a sodium decyl sulfate – decanol – $D_2O$ mixture

O. R. Santos<sup>a,b</sup>, W. S. Braga<sup>a,b</sup>, D. D. Luders<sup>a</sup>, A. R. Sampaio<sup>a</sup>, N. M. Kimura<sup>a</sup>, M. Simões<sup>c</sup>, and A. J. Palangana<sup>a</sup>

<sup>a</sup>Departamento de Física, Universidade Estadual de Maringá, Av. Colombo, Maringá, Paraná, Brazil;

<sup>b</sup>Universidade Tecnológica Federal do Paraná, Campo Mourão, Paraná, Brazil; <sup>c</sup>Departamento de Física, Universidade Estadual de Londrina, Campus Universitário, Londrina, PR, Brazil

### ABSTRACT


The nematic phases of a lyotropic system *NadS*/ decanol/ heavy water are investigated using optical conoscopy and image processing. The phase diagram obtained from these lyotropic materials predicts the occurrence of a direct phase transition, which does not present the biaxial nematic phase, between the discotic ( $N_D$ ) and calamitic ( $N_C$ ) nematic phases. A biaxial nematic ( $N_B$ ) phase is optically characterized and confirmed through conoscopic image, inside the biaxial range, between the two uniaxial nematic phases. Also, their respective transition points are determined by means of image processing. The  $N_B$  phase observed here is discussed as part of the nature of the micellar configuration of lyotropic materials which exhibit uniaxial nematic phases.

### KEYWORDS

uniaxial nematic phases;  
biaxial nematic phase;  
conoscopic image

## Introduction

The first conoscopic images featuring optically biaxial liquid crystals portrayed, a long time ago, a smectic *C* phase, reported by Taylor and co-workers [1], and a biaxial nematic phase ( $N_B$ ) between the discotic ( $N_D$ ) and calamitic ( $N_C$ ) nematic phases, reported by Yu and Saupe [2]. This is an important line of research focusing on biaxial liquid crystal materials that continues to attract the interest of several researchers [3, 4]. In this way, conoscopic image results obtained in lyotropic nematic materials [2, 5] have shown and confirmed the existence of a biaxial nematic domain between uniaxial nematic phases [6 – 10]. Furthermore, the occurrence of a direct transition between the  $N_D$  and  $N_C$  phases, without a biaxial nematic phase between them, was also reported [11 – 13] in a phase diagram obtained from the decyl sulfate (*NadS*), decanol (*DeOH*) and  $D_2O$  mixtures. The optical characterization of the  $N_D$  -  $N_C$  phase transition made by these authors has been basically through optical microscopy observations. We highlight that the schlieren texture, characteristic of these uniaxial nematic phases, is not stable in  $N_D$  phase and, when observed with a polarizing microscope upon heating, it changes to a pseudo-isotropic texture [14]. On the other hand, the schlieren texture is more stable in  $N_B$  and  $N_C$  phases. This means that it is difficult to recognize the  $N_B$  to  $N_C$  transition point, by optical observations between schlieren textures [15, 16]. Thus, it is not

**CONTACT** O. R. Santos ✉ [oscarsantos@utfpr.edu.br](mailto:oscarsantos@utfpr.edu.br)  Departamento de Física, Universidade Tecnológica Federal do Paraná, Caixa Postal 271, 87 301-899, Campo Mourão, PR, Brazil.

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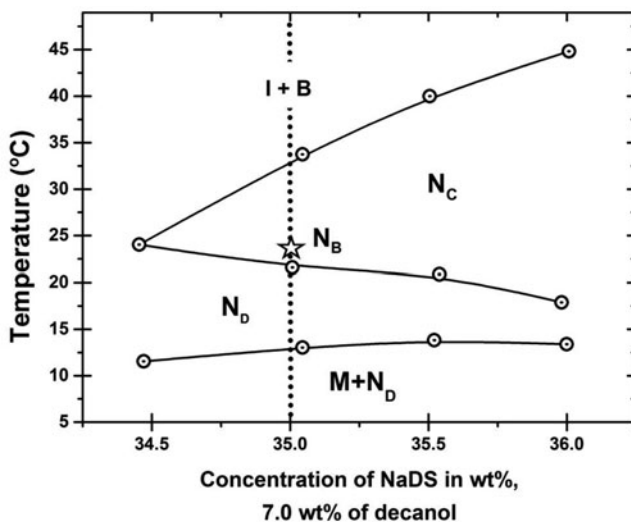
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an easy task into identify the occurrence of a direct transition between  $N_D$  and  $N_C$  phases via optical microscopy. This phase transition is provided in a phase diagram line for a lyotropic mixture of  $NadS$ ,  $DeOH$  and  $D_2O$  compounds. In this context, we present an experimental investigation of the  $N_D$  -  $N_C$  phase transition by optical conoscopy.

The optical conoscopy [17, 18] has been used as a suitable tool to discriminate between uniaxial and biaxial liquid crystal phases [1, 2]. The conosopic image produced by this optical technique in such homeotropic configuration as the uniaxial  $N_D$  phase presents two isogyres known as the Maltese Cross. When the  $N_D$  sample is rotated between crossed polarizers, the conosopic image pattern does not change, which is an optical characteristic of this uniaxial material. The conosopic image observed for a uniaxial sample in a planar configuration as the  $N_C$  phase between crossed polarizers occupies practically the entire field of view in the focal plane of the objective and consists of a very broad, fuzzy isogyre cross. In this way, when the  $N_C$  sample is rotated by a small angle, the isogyre splits and quickly leaves the optical microscopic field of view. Otherwise, for a biaxial  $N_B$  phase, the isogyres open when the sample is rotated, which is the fact used to identify the biaxial phase. In this work, these conosopic images are presented and discussed near the  $N_D$  -  $N_C$  phase transition. The occurrence of a  $N_B$  phase, not provided in this lyotropic material, is clearly identified via conosopic image between two uniaxial nematic ( $N_D$  and  $N_C$ ) phases. In addition, their respective transition points are determined by means of image processing [19, 20].

## Fundamentals

The nematic phases investigated in this work are provided in a phase diagram line [11] (Fig. 1) for a lyotropic mixture (concentration in weight percent) of decyl sulfate ( $NadS$  : 35.0), decanol ( $DeOH$  : 7.0) and deuterium oxide ( $D_2O$  : 58.0). These compounds are commercially available and have been obtained from Aldrich. The nematic phases are characterized by means of optical microscopy, image processing and optical conoscopy techniques. The nematic samples are prepared in sealed glass cells. The 1-2 plane of the sample is defined with



**Figure 1.** Phase diagram extracted from Ref.[11],  $N_D$ ,  $N_B$ ,  $N_C$ ,  $I$ ,  $B$  and  $M$  are the discotic nematic, biaxial nematic, calamitic nematic, isotropic, batonnet and middle soap, respectively. The new biaxial phase here reported, is shown by a star in this figure, between 21.1°C and 21.8°C.

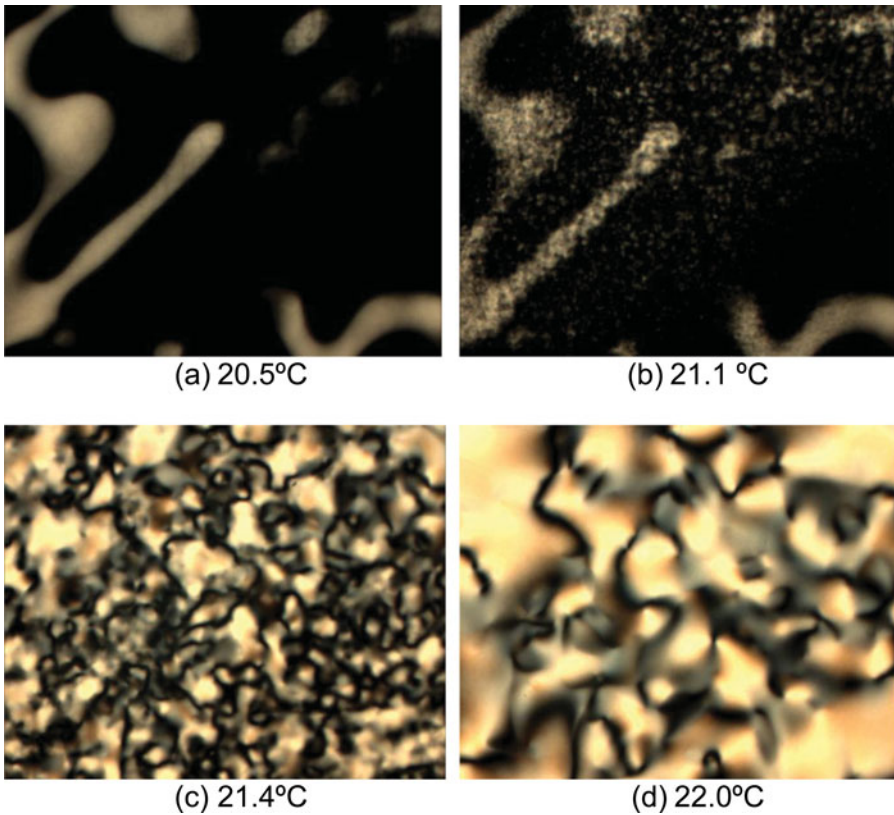
1(2) axis parallel to the length (width) of the cells and 3 is the axis normal to the largest surface of the sample holder. We highlight that the  $N_D$  ( $N_C$ ) phase presents positive (negative) optical birefringence and negative (positive) anisotropy of diamagnetic susceptibility [21]. The  $N_D$  phase is aligned in a homeotropic configuration through a magnetic field ( $\sim 1T$ ) parallel to the 1-axis combined with rotations of the sample nematic around of the 3-axis. Planar alignment of the  $N_C$  phase is obtained via magnetic field ( $\sim 1T$ ) parallel to the 1- axis.

The polarized light optical microscopy connected to the CCD camera (resolution of  $1280 \times 1024$  pixels) is used to observe the nematic textures. Their respective nematic transition points are identified through image processing. A brief summary of the image processing technique is presented here. A more complete study of this technique is found in the references [19, 20]. The image frame of nematic textures is defined by the function  $b(x,y)$ , which represents the 32 bits true pixel color tone that ranges from 0 to 255 in red, green or blue colors (RGB image). The mean intensity of the color tones is given by  $M_0 = 1/l_x l_y \int_0^{l_x} \int_0^{l_y} b(x, y) dx dy$  where  $l_x$  and  $l_y$  are the rectangular dimensions of the image frame. In this way, the 2-rank statistical moments of the image frame are written by  $M_2 = 1/l_x l_y \int_0^{l_x} \int_0^{l_y} [b(x, y) - M_0]^2 dx dy$ . The root square  $(M_2)^{1/2}$  is known as the mean square deviation ( $\sigma$ ) [19, 20]. The parameter  $\sigma$  is determined (Delphi program) as a function of the temperature, for each RGB component of the nematic textures, in the range of nematic phases. We chose, the red color (the most sensitive one), which best identifies the phase transition point via parameter  $\sigma$ , in agreement with other experimental techniques [22, 23].

The optical conoscopy is obtained inserting an Amici-Bertrand lens positioned in the optical system of the polarized light microscope. The interference figure (conoscopic image) of light waves produced by the oriented  $N_D$  sample, in this optical configuration, is observed in the focal plane near the top of the objective. As mentioned before, this conoscopic image is known as the Maltese cross. Its center is called the melatope, corresponding to the optical axis [17, 18]. The conoscopic image characteristic of uniaxial  $N_C$  phase consists of a very broad, fuzzy isogyres cross [17, 18]. The isogyres open when the biaxial liquid crystal sample in thermal equilibrium is rotated from the  $^\circ C$  position. This opening reaches a maximum value when the stage is rotated from the  $45^\circ C$  position [1 – 4, 6 – 10]. We would like to emphasize that the opening of isogyres in uniaxial nematic phases subjected to thermal gradient has been observed [24, 25] while the temperature is changed (in either cooling or heating cycles) with a given rate. This conoscopic image (apparently biaxial) occurs when there is a flow-induced reorientation of the molecules (or micelles) caused by the fluctuation of the thermal expansion coefficient of nematic materials. The conoscopic image with characteristic biaxial, returns to uniaxial nematic (Maltese cross) configurations when the thermal gradient and material flow disappear [24, 25].

## Results and discussion

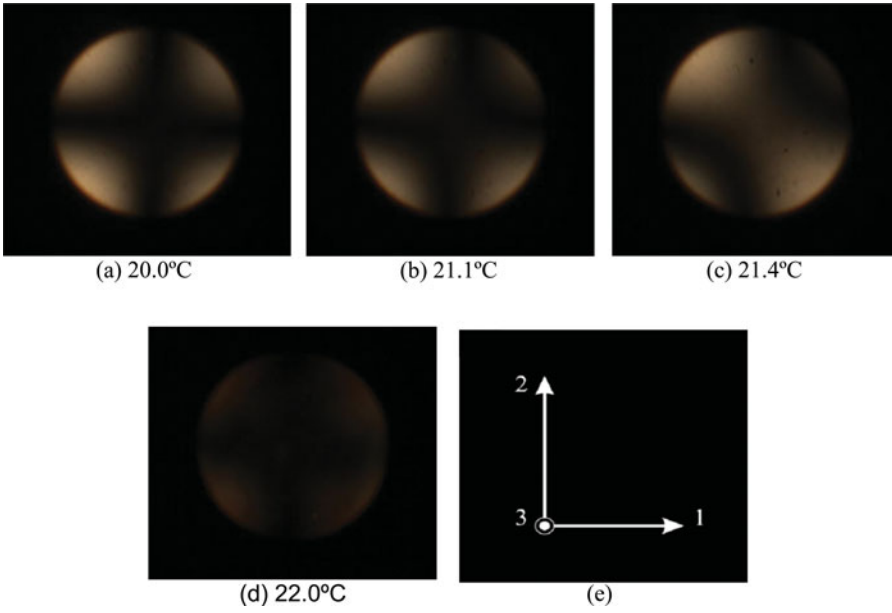
The biaxial nematic range between the  $N_D$  and  $N_C$  phases is presented and discussed now via optical microscopy, optical conoscopy and image processing results. Figure 2 shows the nematic textures obtained upon heating from the  $N_D$  phase, near the  $N_D \rightarrow N_C$  phase transition and  $N_C$  phase. The schlieren texture in  $N_D$  phase is transformed into a pseudo-isotropic texture (see Fig. 2(a)). Note that this texture turns to a bright irregular domain with strong evidence of a  $N_D - N_B$  ( $21.1^\circ C$ ) phase transition [15, 20], as exhibited in Fig. 2(b), and, after the transition is completed, the  $N_B$  phase is characterized by the presence of smooth schlieren texture [15]. The schlieren texture characteristic of the  $N_C$  phase is shown in Fig. 2 (d). It is



**Figure 2.** Nematic textures. (a)  $N_D$  (discotic), (b)  $N_D - N_B$  (biaxial) transition, (c)  $N_B$  and (d)  $N_C$  (calamitic) phases.

important to emphasize that the surface alignment, induced by the boundary conditions, of  $N_C$  ( $N_D$ ) phase is parallel (perpendicular) to the biggest surface of the glass cells while that the surface alignment in the  $N_B$  phase is parallel to the 1 - axis and perpendicular to the 3 - axis [15, 16, 20, and 26]. Therefore, the recognition of the transition point  $N_B$  to  $N_C$  (21.8°C) by optical observations between schlieren textures is difficult to read [15, 16, and 20]. Moreover, our conoscopic image data, discussed below, confirm this phase sequence.

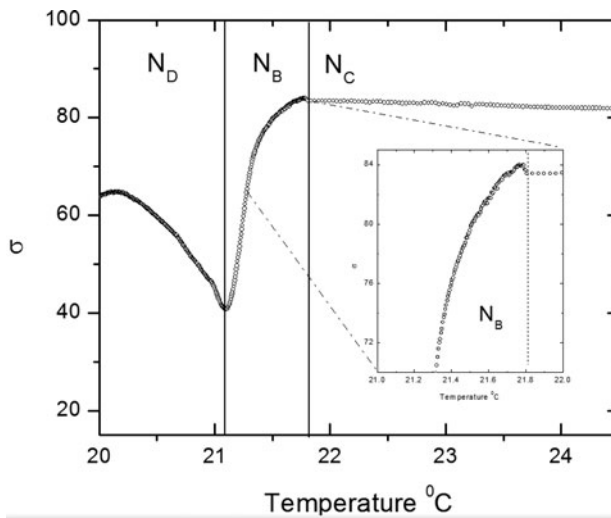
Figure 3 shows the conoscopic images obtained upon heating the discotic nematic near the  $N_D - N_B - N_C$  phase transitions. The conoscopic images, for the  $N_D$  and  $N_B$  phases, are determined when the nematic sample (*in thermal equilibrium*) is rotated (anticlockwise) from the  $0^\circ$  position to the  $45^\circ$  position and then fixed at  $45^\circ$ . The Maltese cross characteristic of the  $N_D$  phase is shown in Fig. 3(a). The isogyres open near the  $N_D - N_B$  phase transition and becomes maximum in the biaxial nematic range and with the melatopes positioned along the NE and SW quadrants as depicted in Fig. 3(b). The  $N_B$  phase is confirmed here by conoscopic image [2, 6]. The  $N_C$  uniaxial phase is optically negative where the conoscopic image consists [7, 8 and 26] of a very broad, fuzzy isogyre cross as exhibited in Fig. 3 (c). In this context, our conoscopic image results clearly indicate the occurrence of a biaxial nematic configuration from a  $N_D$  (homeotropic optical axis) to a  $N_C$  (planar optical axis) phase. The  $N_D - N_B - N_C$  - transition points are determined by image processing [19, 20]. Figure 4 shows the mean square deviation ( $\sigma$ ), obtained from nematic textures, versus temperature near these phase transitions for the heating cycle. Note that  $\sigma$  near the  $N_D - N_B$  phase transition decreases as the temperature increases. This behavior of  $\sigma$  is consistent with the appearance of pseudo-isotropic schlieren texture of  $N_D$  phase. In the biaxial nematic range,  $\sigma$  presents a rapid growth,



**Figure 3.** Conoscopic images of nematic phases. (a)  $N_D$ , (b)  $N_D - N_B$ , (c)  $N_B$ , (d)  $N_C$ , and (e) laboratory frame axis adopted [7].

followed by a slight decrease in direction of the  $N_C$  phase. The growth of  $\sigma$  at  $N_D - N_B$  transition reflects the appearance of bright irregular spots [15, 19, and 20] and subsequently disappears and gradually transforms to a smooth schlieren texture [15, 16] in direction of the  $N_C$  phase. The biaxial nematic phase occurs between two minimum values of  $\sigma$ , corresponding to  $N_D - N_B$  and  $N_B - N_C$  phase transitions in accordance with optical microscopy and optical conoscopy experiments.

In summary, we have carried out an optical conoscopy study near the  $N_D - N_C$  phase transition in a lyotropic mixture of decyl sulfate, decanol and  $D_2O$ . The occurrence of a  $N_B$  phase,



**Figure 4.** Mean square deviation ( $\sigma$ ) versus temperature. The insert shows an enlarged scale, to better observe the  $N_B - N_C$  transition point.



optically characterized through conoscopic image, appears as an intermediate biaxial configuration between the  $N_D$  and  $N_C$  phases. We would like to emphasize that the  $N_B$  phase observed here is part of the micellar configuration of lyotropic materials. The optical conoscopy utilized here is indeed a very useful tool to discriminate between uniaxial and biaxial nematic phases. The image processing is a sensitive technique and is used to detect the uniaxial and biaxial nematic transition points. To the best of our knowledge, this is the first time that this  $N_B$  phase is optically characterized by means of conoscopic images [27]. As a final note, we mention that the experimental result presented and discussed in this work is a complementary study of the Saupe diagram [11] since it does not provide the  $N_B$  phase.

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